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# THERMODYNAMIC INVESTIGATION OF AB AND AB<sub>2</sub> MOLECULAR SPECIES IN BINARY LIQUID SYSTEMS

# EXCESS ENTHALPIES OF 1,4-DIOXANE WITH CHLOROFORM AND BROMOFORM

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#### ABSTRACT

Excess enthalpies have been measured at 308.15 K for 1,4-dioxane (A) + chloroform (B) and 1,4-dioxane (A) + bromoform (B). The data have been examined on the basis of Barker's theory. Interaction energies between the components have been determined and the study suggests that these mixtures contain both AB and  $AB_2$ molecular species.

## INTRODUCTION

Complex formation equilibria in dilute non-electrolyte solutions involving reactions of the type

(1)

in some more or less "inert" solvents have been investigated by various spectroscopic methods as also by such classical thermodynamic methods as distribution between immiscible solvents etc. Hepler and Fenby<sup>1</sup> have recently shown that it is possible to analyse molar excess enthalpies for a binary liquid mixture in terms of equilibrium constant and the molar enthalpy of reaction,  $\Delta H_1^o$ , for the complex formation represented by reaction (1). In a subsequent paper<sup>2</sup> these workers have extended this method to analyse  $H^E$  for mixtures assumed to have AB and AB<sub>2</sub> complexes. In another realistic approach McGlashan and Rastogi<sup>3</sup> have shown that  $K_1$  and  $K_2$ for the reaction

$$A+B \rightleftharpoons AB$$

$$A+2B \stackrel{K_2}{\longrightarrow} AB_2$$

evaluated from vapour pressure measurements can be combined with  $H^{E}$  data to

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yield  $\Delta H_1^\circ$  and  $\Delta H_2^\circ$ . While the most compelling evidence for the presence of AB and AB<sub>2</sub> type molecular species in these mixtures is usually spectroscopic, this is often supplemented by thermodynamic excess functions and their temperature dependence. Excess enthalpies are potentially rich sources of information about complex formation in solution<sup>4-7</sup>. The work described here shows that Barker's theory<sup>8</sup> can be utilized to analyse  $H^E$  data for a binary non-electrolyte mixture to decide whether it contains AB or AB and AB<sub>2</sub> molecular species.

## EXPERIMENTAL

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Dioxane, chloroform and bromoform were purified as suggested by Vogel<sup>9</sup> and the purities of the final samples were checked by measuring their densities as described earlier<sup>10,11</sup>.

Heats of mixing measurements were made in an adiabatic calorimeter<sup>12</sup>.

# RESULTS

Heats of mixing data for various systems are recorded in Table 1. The results were fitted to the expression

$$H^{E}/x_{1}(1-x_{1}) \operatorname{J} \operatorname{mol}^{-1} = h_{0} + h_{1}(2x_{1}-1) + h_{2}(2x_{1}-1)^{2}$$
 (2)

where  $x_1$  is the mole fraction of component 1. The constants  $h_0$ ,  $h_1$  and  $h_2$  were evaluated by fitting  $H^E/x_1(1-x_1)$  to expression (2) by the method of least squares. They are recorded in Table 2 together with the standard deviations  $\sigma(H^E)$ .

## DISCUSSION

Excess enthalpies for 1,4-dioxane (1)+chloroform (2) have been measured at 303.15 and 318.15 K by Van Ness and Abbott<sup>13</sup>. The heats of mixing values for this mixture at 308.15 K interpolated from their data<sup>13</sup> gave values that have a maximum at  $x_2 = 0.6$ ,  $(H_{max}^E = -2080 \text{ J mol}^{-1})$  while our  $H^E$  values have a maximum of  $-2100 \text{ J mol}^{-1}$  at  $x_2 = 0.55$ . Further, while their  $H^E$  values<sup>13</sup> are considerably more endothermic than ours in the composition range  $x_2 = 0.25$  to  $x_2 = 0.45$ , a constant substraction of 200 J mol<sup>-1</sup> from their data well reproduces (within 10 J mol<sup>-1</sup>) our  $H^E$  values in this concentration range. Their  $H^E$  values<sup>13</sup> are also more exothermic than ours in the range  $x_2 = 0.9$ —a constant addition of 120 J mol<sup>-1</sup> to their data also reproduces well within 10 J mol<sup>-1</sup> our  $H^E$  values in this concentration range. We are unaware of any data at 308.15 K with which to compare our results for 1,4-dioxane+bromoform.

The results were examined on the basis of Barker's theory which allows a molecule of type A occupying  $r_A$  sites on a Z-coordinated lattice to have  $q_A^Z = r_A^Z - 2r_A + 2$  neighbouring contact sites; each site having an interaction energy with the neighbouring part of the surface of another molecule. The contact types are further

sub-divided into classes; the number in the  $\mu$ th class of the molecule A denoted by  $Q_{\mu A}$ . As 1,4-dioxane has almost the same molar volume as that of the various solvents used here  $r_A = r_S = 2$  and Z = 4 has been used throughout this paper. Further chloroform and bromoform are assumed to have 2 classes of contact sites, the hydrogen atom is assumed to have one contact  $Q_H$  of one class while the residual part

# TABLE I

# MEASURED HEATS OF MIXING, $H^{E}$ AND COMPARISON OF VALUES CALCULATED ACCORDING TO BARKER'S THEORY AT MOLE FRACTIONS $x_1$ OF COMPONENT 1

<i>x</i> 1	$H^{E}(J \mod^{-1})$		<i>x</i> <sub>1</sub>	$H^{\mathbf{E}}(J mol^{-1})$		
	Exptl.	Barker	•	Exptl.	Barker	
1,4-Dioxan	e (I)+chloroforn	n (2)				
- 			(0.5000)	(-2080)	(-2084.74)	
0.2069	- 1438.47		0.5504	-2015.84	· · ·	
0.2583	-1676.85		0.5975	- 1911.71		
0.2976	-1823.86		0_6717	1678.13		
(0.3000)	(-1850)	(-1830.56)	(0.7000)	(-1580)	(-1573.67)	
0.3200	-1890.91		0.7141	-1504.80	1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 -	
0.3693	-2010.67		0.7458	-1360.36		
0.4129	-2073.10		0.8087	-1050.91	-	
0.4326	-2086.37		0.8412	-876.01		
0.4894	-2082.99				, _	
I.4-Dioxan	e + bromoform					
-•			(0.5000)	(-1830)	(-1839.78)	
0.1608	-1052.37		0.5182	- 1816.04		
0.2314	-1368.98		0.5549	-1782.02	e de la companya de l	
0.2829	-1551.05		0.6030	-1710.05		
(0.3000)	(-1590)	(-1609.20)				
0 3740	-1660.00	( 1005120)	0.6697	-1550.10		
0.52.10			(0.7000)	(-1345)	(-1422.93)	
0.3823	- 1769.88		0.7274	-1383.67		
0.4008	-1799.02		0.7761	-1178.89		
0.4536	-1834.13		0.8535	-876.77	•	
0.4987	-1829.60					

# TABLE 2

# PARAMETERS OF EQN (2) TOGETHER WITH THE STANDARD DEVIATIONS $\sigma(H^{\pm})$ AND INTERACTION ENERGIES

	h <sub>o</sub>	<i>h</i> 1	h2	σ(H <sup>E</sup> ) (J mol <sup>-1</sup> )	U <sub>1</sub> (J mol <sup>-1</sup> )	U <sub>2</sub> (J mol <sup>-1</sup> )	U <sub>3</sub> (J mol <sup>-1</sup> )
1,4-Dioxane+ chloroform	-8313.47	1588.31	1421.26	1.54	230.29	-4903.43	- 5889.94
1,4-Dioxane+ bromoform	-7320.18	848.41	213.29	2.19	230.29	4617.98	-5319.15

has 5 contact point  $Q_x$  of another class. Again 1,4-dioxane is assumed to have two classes of contact sites, the two oxygen atoms having contacts of one class while the residual part having contact sites of another class. The interactions considered were a specific (O-H) interaction between the oxygen atoms of 1,4-dioxane and the proton of the haloforms and of strength  $U_2$ ; all the non-specific interactions, for the sake of simplicity, are assumed to have the same strength  $U_1$ . Interactions between contact sites of the same class are taken to have zero interaction energy.

For 1,4-dioxane+chloroform, the two oxygen atoms of dioxane were first assumed to have 4 contact sites  $Q_{OA}$  of one class and the residual part R has 2 contact sites of another class. Excess energy of mixing at constant volume  $U_v^E$  values were then evaluated from the expression

$$U_{V}^{E} = -2RT[(x_{O}x_{x} + x_{R}x_{H} + x_{R}x_{x})\eta_{1} \ln \eta_{1} + \eta_{2} \ln \eta_{2}(x_{O}x_{H})]$$
(3)

where the various parameters x depend upon the number of interactions of various contact sites of different classes in molecules A and B of the binary mixture in the manner described in ref. 8. These parameters were evaluated by solving the following simultaneous quadratic eqns (4)-(7) with certain assumed values of  $U_1$  and  $U_2$ .

$$x_{0}[x_{0} + \eta_{1}x_{R} + \eta_{2}x_{H} + \eta_{1}x_{r}] = Q_{0A}x_{A/2}$$
(4)

$$x_{R}[\eta_{1}x_{O} + x_{R} + \eta_{1}x_{H} + \eta_{1}x_{I}] = Q_{RA}x_{A/2}$$
(5)

$$x_{\rm H}[\eta_2 x_{\rm O} + \eta_1 x_{\rm R} + x_{\rm H} + \eta_1 x_{\rm x}] = Q_{\rm HB} x_{\rm B/2}$$
(6)

$$x_{x}[\eta_{1}x_{0} + \eta_{1}x_{R} + \eta_{1}x_{H} + x_{x}] = Q_{XB}x_{B/2}$$
(7)

where  $\eta_i = \exp(-U_i/RT)$  (i = 1 or 2),  $U_1$  and  $U_2$  are the interaction energies (per mole),  $x_A$  is the mole fraction of A and R is the gas constant. It was found that no values of  $U_1$  and  $U_2$  gave  $U_V^E$  values in this case that came any close to the experimental  $H^E$  values for this mixture.

The two oxygen atoms of 1,4-dioxane in dioxane+chloroform were then assumed to have 2 contact sites  $Q_{0A}$  of one class and the residual part R has 4 contact sites  $Q_{RA}$  of another class.  $U_V^E$  values were then calculated from expression (3) in the manner described above.  $U_V^E$  values at  $x_1 = 0.3$ , 0.5 and 0.7 for the best  $U_1$  and  $U_2$ values of 230.29 and  $-5084.98 \text{ J} \text{ mol}^{-1}$  were -1546.27, -2058.14 and -1033.05 Jmol<sup>-1</sup>, respectively. Neglecting the contributions of volume change of mixing  $V^E$ , to  $U_V^E$ , we take  $U_V^E \approx H^E$  and so that these  $U_V^E$  values at  $x_1 = 0.3$ , 0.5 and 0.7 now make a better reproduction of  $H^E$  data for 1,4-dioxane+chloroform. The theoretical reproduction of the experimental  $H^E$  data for this mixture is not good in either of these two cases, the latter being a better one. The failure in the latter case may be due to the assumption 'hat the oxygen atoms of 1,4-dioxane have contacts of one type only.

We now suppose that the two oxygen atoms of 1,4-dioxane in dioxane+chloroform have 2 contact sites of the same class but of two different subclasses. Either one or both of these sites on the two oxygen atoms of dioxane may be involved in its interaction with chloroform. The interaction, when only one oxygen atom of 1,4dioxane is involved with chloroform, i.e.,  $Q_{OA} = 1$ , is assumed to have an interaction energy of  $U_2$  while that when both of the contact sites on the two oxygen atoms of 1,4-dioxane are involved, i.e.,  $Q_{OIA} = 2$ , is taken to have an interaction energy of  $U_3$ . The proton interacting with  $Q_{OA}$  is designated as H while that interacting with  $Q_{OIA}$  is labelled at H<sup>1</sup>. If 1,4-dioxane+chloroform contains both AB and AB<sub>2</sub> complex species in solution,  $U_y^E$  would be expressed by

$$U_{v}^{E} = -2RT[(x_{0}x_{x} + x_{0}, x_{x} + x_{R}x_{H} + x_{R}x_{H}, y_{1} \ln \eta_{1} + (x_{0}x_{H})\eta_{2} \ln \eta_{2} + (x_{0}, x_{H})\eta_{3} \ln \eta_{3}]$$
(8)

where the various parameters were evaluated by solving the following simultaneous quadratic eqns (9)–(14) for certain assumed values of  $U_1$ ,  $U_2$  and  $U_3$ .

$$x_{O}[x_{O} + \eta_{1}x_{O^{1}} + \eta_{1}x_{R} + \eta_{2}x_{H} + \eta_{2}x_{H^{1}} + \eta_{1}x_{r}] = Q_{OA}x_{A/2}$$
(9)

$$x_{01}[\eta_1 x_0 + x_{01} + \eta_1 x_R + \eta_3 x_H + \eta_3 x_{H1} + \eta_1 x_z] = Q_{01A} x_{A/2}$$
(10)

$$x_{R}[\eta_{1}x_{0}+\eta_{1}x_{0}+x_{R}+\eta_{1}x_{H}+\eta_{1}x_{H}+\eta_{1}x_{z}] = Q_{RA}x_{A/2}$$
(11)

$$x_{\rm H}[\eta_2 x_{\rm O} + \eta_2 x_{\rm O1} + \eta_1 x_{\rm R} + x_{\rm H} + \eta_1 x_{\rm H1} + \eta_1 x_{\rm I}] = Q_{\rm HB} x_{\rm B/2}$$
(12)

$$\mathbf{x}_{\mathrm{H}^{1}}[\eta_{3}\mathbf{x}_{0} + \eta_{3}\mathbf{x}_{0^{1}} + \eta_{1}\mathbf{x}_{\mathrm{R}} + \eta_{1}\mathbf{x}_{\mathrm{H}} + \mathbf{x}_{\mathrm{H}^{1}} + \eta_{1}\mathbf{x}_{\mathrm{x}}] = Q_{\mathrm{H}^{1}\mathrm{B}}\mathbf{x}_{\mathrm{B}/2}$$
(13)

$$\mathbf{x}_{\mathbf{x}}[\eta_{1}\mathbf{x}_{0} + \eta_{1}\mathbf{x}_{0^{1}} + \eta_{1}\mathbf{x}_{R} + \eta_{1}\mathbf{x}_{H} + \eta_{1}\mathbf{x}_{H^{1}} + \mathbf{x}_{\mathbf{x}}] = Q_{\mathbf{x}\mathbf{B}}\mathbf{x}_{\mathbf{B}/2}$$
(14)

 $U_V^E$  values evaluated in this manner for  $x_1 = 0.3$ , 0.5 and 0.7 are recorded in Table 1 and they well reproduce the experimental  $H^E$  curve for this mixture. The analysis of  $H^E$  data for dioxane + chloroform in terms of the Barker's theory thus suggests that this mixture contains both AB and AB<sub>2</sub> molecular species in solution. These species would persist even to great dilution as Matsui et al.<sup>14</sup> have maintained in their analysis of their infinite dilution partial molar enthalpy of a binary solution containing dimethyl sulphoxide (A) and chloroform (B).

 $U_v^E$  values for 1,4-dioxane+bromoform were also analysed in the manner as described for 1,4-dioxane+chloroform. It was again observed that the assumption that this mixture also contains AB and AB<sub>2</sub> molecular species in solution yielded  $U^E$  values that reproduce pretty well  $H_v^E$  data for this mixture.

Examination of  $U_2$  values for 1,4-dioxane+chloroform and 1,4-dioxane+ bromoform shows that compared to bromoform, chloroform forms a stronger Hbond with 1,4-dioxane. The bromines in bromoform due to their size are not able to displace the charge on the C-H bond to such an extent as the chlorines in chloroform and consequently bromoform would form a weaker H-bond with dioxane. This should also be evident in H-bond formation in AB<sub>2</sub> species in these mixtures and the  $U_3$  interaction energies support this conjecture.

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